$\tau(p)/p = 1883882662835292$ , which ratio is not itself divisible by p. The ratio  $\tau(p) \pmod{p}/p$  appears to be distributed uniformly between 0 and 1. That implies that the number of such "Newman primes" (i.e., 2, 3, 5, 7, 2411,...) that do not exceed N should be asymptotic to  $\sum_{p \le N} (1/p) \sim \ln \ln N$ . Since the normal order of magnitude of  $\tau(p)$  is  $\pm p^{11/2}$ , and since there are no other Newman primes  $\leq$ 16067, it is therefore very improbable that  $\tau(n)$ , which is multiplicative, will have a zero.

D. S.

## 10 [9].—SAMUEL YATES, Prime Period Lengths, RCA Defense Electronic Products, Moorestown, New Jersey. Ms. (undated) of 525 pp. deposited in the UMT file.

This voluminous unpublished table gives the length of the decimal period of the reciprocal of each of the 105000 odd primes (excluding 5) from 3 to 1370471, inclusive. This compilation evolved over the past four years from calculations performed on a succession of electronic computers such as IBM 7090, XDS Sigma 7, RCA Spectra 70/45, and (mainly) RCA Spectra 70/55 at the Moorestown computer facility.

The author has supplied supplementary detailed information relating to the density of those tabulated primes having 10 as a primitive root, from which we find, for example, that there are precisely 39447 such primes in the tabular range. On the other hand, Artin's conjecture [1] predicts a count of 39266 in the same range; however, there exists heuristic reasoning [2] to support the observation that the density of such primes generally exceeds the predicted density. (This reviewer has found the first exception to occur for the interval ending with the prime 138289.) It may be noted here that Cunningham [3] erroneously gave 3618, instead of 3617, as the count of such primes less than 10<sup>5</sup>. Also, D. H. Lehmer & Emma Lehmer [4] reported a count of 8245 such primes below 2.5 · 10<sup>5</sup>, attributed to Miller, but the latter in an unpublished table [5] has given this count as 8255, in agreement with one based on the present table.

The range of this new table is more than tenfold that of any of the previous tables of this type, as listed by Lehmer [6]. The table has materially assisted its author in his continuing search for new prime factors of integers of the form  $10^n - 1$  [7].

J. W. W.

2. DANIEL SHANKS, Solved and Unsolved Problems in Number Theory, Spatian BOOKS, Washington, D.C., 1962, pp. 80-83.
3. A. CUNNINGHAM, "On the number of primes of the same residuacity," Proc. London Math. Soc., (2), v. 13, 1914, pp. 258-272.
4. D. H. LEHMER & EMMA LEHMER, "Heuristics, anyone?," Studies in Mathematical Analysis and Related Topics, Stanford Univ. Press, Stanford, Calif., 1962, pp. 202-210.
5. J. C. P. MILLER, Primitive Root Counts, University Mathematical Laboratory, Cambridge, England. Ms. deposited in UMT file; Math. Comp., v. 26, 1972, p. 1024, RMT 54.
6. D. H. LEHMER, Guide to Tables in the Theory of Numbers, National Research Council 6. D. H. LEHMER, Guide to Tables in the Theory of Numbers, National Research Council

Bulletin No. 105, Washington, D.C., 1941, p. 15. 7. SAMUEL YATES, Partial List of Primes with Decimal Periods Less than 3000, Moorestown, New Jersey, Ms. deposited in UMT file; Math. Comp., v. 26, 1972, p. 1024, RMT 55.

## 11 [10].—P. A. MORRIS, Self-Complementary Graphs and Digraphs, 24 pp. deposited in the UMT file.

Two graphs, G and  $\overline{G}$ , on the same set of nodes, are *complementary* if two nodes are joined in G if, and only if, they are not joined in  $\overline{G}$ . Two digraphs D and  $\overline{D}$ , on

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<sup>1.</sup> A. E. WESTERN & J. C. P. MILLER, Tables of Indices and Primitive Roots, Royal Society Mathematical Tables, v. 9, Cambridge Univ. Press, London, 1968, p. xli. 2. DANIEL SHANKS, Solved and Unsolved Problems in Number Theory, Spartan Books,